

## Trigonometric Identities

$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$ $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$ $\sin(A + B)\sin(A - B) = \sin^2 A - \sin^2 B = \cos^2 B - \cos^2 A$ $\cos(A + B)\cos(A - B) = \cos^2 A - \sin^2 B = \cos^2 B - \sin^2 A$ $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$ $\cot(A \pm B) = \frac{\cot A \cot B \mp 1}{\cot B \pm \cot A}$ $2 \sin A \cos B = \sin(A + B) + \sin(A - B)$ $2 \cos A \sin B = \sin(A + B) - \sin(A - B)$ $2 \cos A \cos B = \cos(A + B) + \cos(A - B)$ $2 \sin A \sin B = \cos(A - B) - \cos(A + B)$ $\sin C + \sin D = 2 \sin \frac{C + D}{2} \cos \frac{C - D}{2}$ $\sin C - \sin D = 2 \cos \frac{C + D}{2} \sin \frac{C - D}{2}$ $\cos C + \cos D = 2 \cos \frac{C + D}{2} \cos \frac{C - D}{2}$ $\cos D - \cos C = 2 \sin \frac{C + D}{2} \sin \frac{C - D}{2}$ $\sin 2A = 2 \sin A \cos A ; \cos 2A = \cos^2 A - \sin^2 A$ $\tan 2A = \frac{2 \tan A}{1 - \tan^2 A} ; \cot 2A = \frac{\cot^2 A - 1}{2 \cot A}$ $\sin 2A = \frac{2 \tan A}{1 + \tan^2 A} ; \cos 2A = \frac{1 - \tan^2 A}{1 + \tan^2 A}$ $1 - \cos 2A = 2 \sin^2 A ; 1 + \cos 2A = 2 \cos^2 A$ $\frac{1 - \cos 2A}{1 + \cos 2A} = \tan^2 A$ $\sin 3A = 3 \sin A - 4 \sin^3 A ; \cos 3A = 4 \cos^3 A - 3 \cos A$ $\tan 3A = \frac{3 \tan A - \tan^3 A}{1 - 3 \tan^2 A}$ $\sin \theta = 2 \sin \frac{\theta}{2} \cos \frac{\theta}{2} ; \cos \theta = \cos^2 \frac{\theta}{2} - \sin^2 \frac{\theta}{2}$ $1 + \cos \theta = 2 \cos^2 \frac{\theta}{2} ; 1 - \cos \theta = 2 \sin^2 \frac{\theta}{2}$ $\tan \theta = \frac{2 \tan \frac{\theta}{2}}{1 - \tan^2 \frac{\theta}{2}} ; \sin \theta = \frac{2 \tan \frac{\theta}{2}}{1 + \tan^2 \frac{\theta}{2}} ;$ $\cos \theta = \frac{1 - \tan^2 \frac{\theta}{2}}{1 + \tan^2 \frac{\theta}{2}}$	$\sin \theta = 0 \text{ n}\pi, \theta = n\pi ; \tan \theta = 0 \text{ n}\pi, \theta = n\pi ;$ $\cos \theta = 0 \text{ n}\pi, \theta = (2n + 1)\frac{\pi}{2} ;$ $\sin \theta = 1 \text{ n}\pi, \theta = (4n + 1)\frac{\pi}{2} ;$ $\sin \theta = -1 \text{ n}\pi, \theta = (4n - 1)\frac{\pi}{2} ;$ $\cos \theta = 1 \text{ n}\pi, \theta = 2n\pi$ $\cos \theta = -1 \text{ n}\pi, \theta = (2n + 1)\pi ;$ $\sin \theta = k = \sin \alpha \text{ n}\pi, \theta = n\pi + (-1)^n \alpha$ $\cos \theta = k = \cos \alpha \text{ n}\pi, \theta = 2n\pi \pm \alpha$ $\tan \theta = k = \tan \alpha \text{ n}\pi, \theta = n\pi + \alpha$ $\sin^{-1} x = \cos ec^{-1} \frac{1}{x} ; \cos ec^{-1} x = \sin^{-1} \frac{1}{x}$ $\cos^{-1} x = \sec^{-1} \frac{1}{x} ; \sec^{-1} x = \cos^{-1} \frac{1}{x}$ $\tan^{-1} x = \cot^{-1} \frac{1}{x} ; \cot^{-1} x = \tan^{-1} \frac{1}{x}$ $\sin^{-1} x = \cos^{-1} \sqrt{1 - x^2} ; \cos^{-1} x = \sin^{-1} \sqrt{1 - x^2}$ $\sec^{-1} x = \tan^{-1} \sqrt{x^2 - 1} ; \tan^{-1} x = \sec^{-1} \sqrt{1 + x^2}$ $\cos ec^{-1} x = \cot^{-1} \sqrt{x^2 - 1} ; \cot^{-1} x = \cos ec^{-1} \sqrt{1 + x^2}$ $\tan^{-1} x \pm \tan^{-1} y = \tan^{-1} \frac{x \pm y}{1 \mp xy}$ $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \tan^{-1} \frac{x + y + z - xyz}{1 - yz - zx - xy}$ $2 \tan^{-1} x = \tan^{-1} \frac{2x}{1 - x^2} = \sin^{-1} \frac{2x}{1 + x^2} = \cos^{-1} \frac{1 - x^2}{1 + x^2}$ $\sin^{-1} x \pm \sin^{-1} y = \sin^{-1} \left\{ x\sqrt{1 - y^2} \pm y\sqrt{1 - x^2} \right\}$ $\cos^{-1} x \pm \cos^{-1} y = \cos^{-1} \left\{ xy \mp \sqrt{1 - x^2} \sqrt{1 - y^2} \right\}$ $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = 2R$ $\cos A = \frac{b^2 + c^2 - a^2}{2bc} ; \cos B = \frac{c^2 + a^2 - b^2}{2ca}$ $\cos C = \frac{a^2 + b^2 - c^2}{2ab} ; a = b \cos C + c \cos B$ $b = c \cos A + a \cos C ; c = a \cos B + b \cos A$ $\Delta = \frac{1}{2} bc \sin A = \frac{1}{2} ca \sin B = \frac{1}{2} ab \sin C$ $\Delta = \sqrt{s(s - a)(s - b)(s - c)}$
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